



Forest inventory estimation using remotely sensed data as a stratification tool - a simulation study

Fredrik Norström

Arbetsrapport 96 2002
Working Paper 96 2002

SWEDISH UNIVERSITY OF
AGRICULTURAL SCIENCES (SLU)

Department of Forest Resource
Management and Geomatics
S-901 83 UMEÅ

Phone: 090-786 58 25 Fax: 090-14 19 15, 77 81 16

ISSN 1401-1204

ISRN SLU-SRG-AR--96 --SE

Abstract

It is well known that remotely sensed data and forest variables are correlated. For inventories like the Swedish National Forest Inventory (NFI) covering large geographic areas, the design for the sample plot layout is often either systematic sampling or simple random sampling. It is reasonable to assume that the design could be more cost efficient if remotely sensed data are used as auxiliary information. A simulated model has been constructed to evaluate the gain in precision when stratified sampling, based on remotely sensed data, is used.

A grid map was created to correspond with a landscape in the northern part of Sweden. First, the map area was divided into forest stands, and a vegetation class was assigned randomly according to a probability distribution obtained using NFI data from Norrbotten and Västerbotten counties, Sweden. Thereafter, for each grid element of the map both wood volume and spectral values were simulated. The wood volumes were simulated using field data from the NFI and the spectral values were simulated with a regression function based on the wood volumes that correspond to a Landsat TM scene with a $30\text{m}\times 30\text{m}$ resolution.

Based on the spectral values the grid elements were classified into different strata. Stratified sampling was then performed and compared with simple random sampling without replacement. The comparisons show that the stratified sampling, based on remotely sensed data, produce much more precise inventory estimates of volume than simple random sampling.

1 Introduction

In recent years, the quality of remotely sensed data has improved, and, in combination with better computing resources, the possibilities for ground predictions have increased. This has also led to the possibility of using remotely sensed data as a stratification tool for improving the precision of inventory estimates. In Poso *et al.* (1987) the stratification approach, with unsupervised classifications, was used in a two-phase design to increase the precision of inventory estimates of volume and age under relatively small scale study conditions in Finland. In McRoberts *et al.* (2002) the stratification approach was used to improve the precision of forest area estimates in the states of Indiana, Iowa, Minnesota and Missouri in the United States. In this study a flexible simulation model was introduced. It was developed so that it was possible to both evaluate forest area estimates with stratified sampling and to check how the different components of the constructed model affect the stratification result. It is also possible to use the model for variables other than the wood volume, which was considered here.

The Swedish National Forest Inventory (NFI) is an inventory covering a large geographic area. It is an inventory incorporating field data from the whole of Sweden for many forest variables and also for some nonforest variables. The NFI started in 1923 and a systematic design of clusters, chosen with systematic sampling, has been used since 1953. Remotely sensed data have not been invoked yet but that is an option for the design in the future.

The effects of stratified sampling, for inventories like the NFI were evaluated with a simulation model. In the model, a grid-based map with values of field data and remotely sensed data corresponding to the Swedish counties Norrbotten and Västerbotten (see *Figure 1*), was created. Initially an area was divided into polygons, with each polygon created to correspond

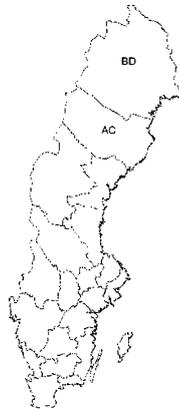


Figure 1, map of Sweden, BD - Norrbotten and AC - Västerbotten. Courtesy © Lantmäteriverket 1998. Ur GSD - Blå [alt.] Gröna kartan, dnr 507-98-4720.

to a forest stand. For each stand a vegetation class was assigned according to a probability distribution obtained from NFI data recorded from Norrbotten and Västerbotten counties. The stand map was created using two different tessellation methods, namely the standard Poisson process and a Dirichlet cells approach. The map polygons for these two methods differ, both in shape and size. It is therefore possible to draw conclusions about the effect on the variance of the stratified sampling when different methods are used to create the polygons.

For each grid element of the forest stand map, field data were simulated to correspond to wood volume in areas from the northern part of Sweden. The simulated wood volumes were based on field data from the NFI between 1993 and 1998. With a regression function based on the wood volume, developed by Nilsson and Ranneby (1997), the remotely sensed data were simulated to correspond to the spectral values of a Landsat TM scene.

In order to investigate whether stratified sampling could be useful for the Swedish NFI, stratified sampling and simple random sampling without replacement were compared for the simulated map. The strata were created from the remotely sensed data using a contextual classification method. This classification method was based not only on information about the pixel itself, but also on information about the classes and the data in the neighboring pixels. The comparisons were done under different conditions as described in Section 4.

2 Field data and remotely sensed data

The field data were based on data collected between 1993 and 1998 by the NFI in the northern part of Sweden for the land use class “forest”. The “forest” was used, as digital map information is available to define the “forest” on a remotely sensed image. The simulated data could be seen as a map filtered from land use classes other than forest. The sample plots of the NFI are located systematically along the sides of a squared cluster called “tracts” (Ranneby *et al.*, 1987). Each tract consists of either twelve temporary plots with radii of 7 meters or eight permanent plots with radii of 10 meters. The permanent plots are remeasured every fifth year whilst the temporary plots are measured only once. The field data in this study were based on the temporary plots.

The remotely sensed data were based on a Landsat TM scene acquired over Sweden on 6 July 1991 (path 194, row 15), geometrically precision corrected to the Swedish National Grid. In order to reduce the computing time only bands 4 and 5 of the Landsat TM bands were used, as they are known to be most useful for prediction of wood volume.

3 Simulation study

Maps with simulated values of wood volume per hectare and spectral reflectances for elements corresponding to a pixel were created. The objective was to construct guidelines for an efficient design for the NFI and similar inventories; a design using remotely sensed data as auxiliary information. The simulation study was built up in 4 main steps:

- Construction of a grid-based map with areas divided into polygons, which are randomly assigned to a forest stand class.
- Simulation of field data for each pixel in the map.
- Simulation of spectral values for each pixel in the map.
- Classification of each pixel into an age class, and performance of stratified sampling on the classes.

3.1 The map

To make possible the evaluation of different sampling strategies, a forest stand map, corresponding to a hypothetical area in the northern part of Sweden, was created. The map was

divided into 480×480 quadratic pixels each of area 900 m^2 . Each pixel consisted of 6 rectangular sample plots, each with an area of 150 m^2 . Pixel size was determined to correspond to the size of a Landsat TM scene, and each sample plot corresponded in size to a temporary sample plot of the Swedish NFI. The average stand size on the map was alternated at three levels, 7.3, 14.6 and 29.2 hectares/stand, where the 14.6 hectare level is the one best corresponding to the true stand size. To simulate a map with these average stand sizes, and also with a good distribution of the sizes and shapes of the stands, two different approaches were tested. One map was created from a Dirichlet cells approach and the other using the standard Poisson lines process. With both techniques each pixel contained 25 grid elements. The pixels were divided into grid elements to retain information about the location of a potential border in the pixel. After the stands were generated, the identities of the 6 sample plots within a pixel were decided from the 25 grid elements of the pixel. The class identities of the plots within each pixel were defined based on the proportions of each class among the 25 grid elements.

The Dirichlet cells approach started with simulation of points from a Poisson point process with intensity λ . At a location equidistant from two neighboring points, borders were created, and at the same time a polygon net developed. Each pixel of the map was assigned to the polygon in which it was placed, see *Figure 2*. Theoretical properties of the Dirichlet cells (also called Voronoi diagrams) and their simulation are described in Okabe *et al.* (2000).

For the standard Poisson line process a line a with a uniformly distributed length l between 0 and $\sqrt{2} \times 1200$ and a uniformly distributed angle θ between 0 and 2π was simulated. A second line b was drawn perpendicular to a . If any part of the line b was inside the region $[-1200,1200] \times [-1200,1200]$ (that region was used due to the map size of 2400×2400 pixels) it was used to create polygons. The number of lines b to be generated with this approach was simulated from a Poisson distribution with intensity μ . A polygon net was generated from the m lines that were retained, see *Figure 3*.

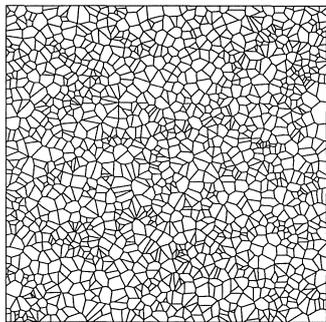


Figure 2. Grid-based map created with the Dirichlet cells technique.

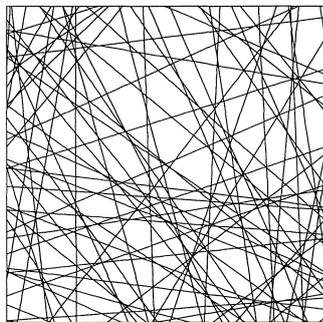


Figure 3. Grid-based map created with the Standard Poisson line process.

The statistical properties of the Poisson line process were first considered by Goudsmit (1945) and the statistical properties have since been investigated by Miles (1964a,b). Statistical properties for the generation of polygons from the Poisson line process are summarized in Santalo (1979) and an algorithm for the generation of the standard Poisson process is included in Crain and Miles (1976).

The two techniques for creating polygons will give polygons with different properties. The standard Poisson line process will generate many small and a few relatively large polygons compared to the Dirichlet cells approach which tends to give polygons more similar in size. The polygons of the standard Poisson line approach will also be narrower and also longer than those from the Dirichlet cells approach which are more circular in shape. Every polygon in each map was developed to correspond to a forest stand, and was assigned an age class with three different probabilities of the youngest age class relative to the other classes. In the first case considered, the probabilities were based on the empirical distribution for the classes, i.e. the proportions of each class in the NFI data. In the second case the probability of assigning a polygon of the youngest age class was decreased, whilst in the third this probability was increased, in comparison with the empirical distribution. The probabilities of the other classes in the later two cases had the same relation between them as the first case with the exception of last case where class 2 had to be revised to a higher probability at the expense of class 3 to avoid numerical difficulties. The probabilities for each of the three cases are given in *Table 1*. The following four age intervals were used, 0-10, 11-30, 31-80, and > 80 years.

	0-10	11-30	31-80	> 80
empirical	0.121	0.049	0.437	0.393
more old forest	0.050	0.053	0.473	0.425
more young forest	0.200	0.050	0.392	0.358

Table 1

3.2 Wood volumes

For each grid element of the forest stand map, field data were simulated to correspond to wood volume in areas from the northern part of Sweden. The wood volumes were obtained by a three-step approach based on NFI data from 1993 to 1998. In the first step, for each forest stand with a given age class c , a sample s of size $k=50$ was drawn from each forest stand given an age class c in the NFI data. k elements, instead of the whole NFI data of the class, were used to make it possible to develop stands of the same age class but with different statistical properties applying to the sample. Secondly, for every sample plot of the stand, one observation was drawn randomly from the sample s . To create wood volumes over an area corresponding to a pixel the sample plots within the pixel were thereafter averaged. The size of the pixel was determined to correspond to a pixel in a Landsat TM scene to make possible the inclusion of remotely sensed data in the sample design. The area of each pixel was $30m \times 30m$.

In the third step the spatial dependency was incorporated. Spatial dependency models are necessary owing to the distance dependency that exists in the forest. This dependency was investigated by Wallerman *et al.* (2001) with semivariograms from the Brattåker area in the Västerbotten county, Sweden. Using equation (1) below the wood volumes, $\nu_{i,j}$, were adjusted for the spatial dependency. The map created consisted of 480 elements (pixels) in both horizontal and vertical directions, and equation (1) was performed for all elements except the map borders:

$$\nu_{adj,i,j} = w_1\nu_{i,j} + w_2\nu_{i-1,j} + w_3\nu_{i,j+1} + w_4\nu_{i+1,j} + w_5\nu_{i,j-1},$$

$$i = 2, \dots, 479, j = 2, \dots, 479, \tag{1}$$

where $\sum_{k=1}^5 w_k = 1$, all weights w_k are chosen to be positive, i is the position in the east-west direction and j is the position in the north-south direction of the map. *Figure 4* and *Figure 5*

give a picture of the amounts of wood volume for both map approaches.

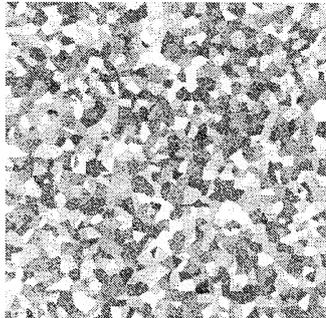


Figure 4. Contour map of amount of wood volume, created with the Dirichlet cells technique.

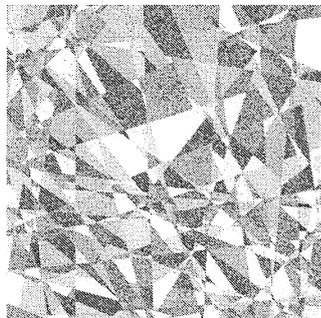


Figure 5. Contour map of amount of wood volume, created with the Standard Poisson line process.

The spatial dependency model was validated with the semivariograms mentioned above. These agreed well with those from the simulated data and the weights $w_1 = 0.8$ and $w_k = 0.05$, $k=2, \dots, 5$ best fitted to the data. To check the influence of the spatial dependency model for different settings the weights $w_1 = 0.9$ and $w_k = 0.025$, $k=2, \dots, 5$ were used also.

3.3 Spectral values

The spectral values were simulated as a function of wood volume ν using a regression technique. Nilsson and Ranney (1997) constructed the regression model used to create pixelwise simulated spectral values for bands 1-5 and 7 of a Landsat TM image. The model was:

$$DN_i = e^{\alpha_i + \beta_i \ln(\nu) + \zeta_i}, i = 1 - 5, 7, \quad (2)$$

where DN_i denotes the digital numbers, i denotes the spectral band and ζ_i are correlated random errors for the spectral bands. The unknown parameters α_i and β_i , $i=1-5,7$, and the unknown covariance matrix $\Sigma_{i,j}$, $i,j=1-5,7$, of the correlated random components ζ_i , $i=1-5,7$, in this study were estimated from a Landsat TM scene, see Nilsson and Ranney (1997).

3.4 Sampling

With a simulated map, it is possible to compare traditional sampling designs, such as systematic sampling and simple random sampling without replacement, with sampling designs using remotely sensed data as auxiliary information. The spectral values were used to assign every pixel to a stratum, with the stratum based on the same age classes as in Section 3.1. After the classification, stratified sampling with both proportional and optimal allocation was applied.

3.5 The classification method

For the created map, the neighboring pixels are dependent and it is therefore reasonable to use a Bayesian contextual classification method. The contextual methods differ from non-contextual classification methods in that they do not only classify on the basis of the pixel itself, but information from neighboring pixels also influences the result. Several authors have developed contextual methods, for example Owen and Switzer (1982); Haslett (1985); Kartikeyan *et*

al. (1994); Sharma and Sarkar (1998); Khazenie and Crawford (1990); Watanabe *et al.* (1994) and Flygare (1993).

For a contextual classification method it is often assumed that the feature vector is a sum of two independent components, where the data are influenced by the classes and the first order neighbors:

$$\mathbf{X}_{i,j} = \mathbf{Y}_{i,j} + \boldsymbol{\varepsilon}_{i,j}, \quad (3)$$

where $\mathbf{X}_{i,j}$ is the observed spectral reflectance, $\mathbf{Y}_{i,j}$ is the true spectral reflectance and $\boldsymbol{\varepsilon}_{i,j}$ is the class independent, possibly spatially correlated, noise. The vectors $\mathbf{Y}_{i,j}$ are assumed to be conditionally independent given their classes. A model for the classifications is:

$$\mathbf{Y}_{i,j}|C_{i,j} = k \sim N(\mu_k, (1 - \theta)\boldsymbol{\Sigma}), \quad (4)$$

$$\boldsymbol{\varepsilon}_{i,j} \sim N(0, \theta\boldsymbol{\Sigma}), \quad (5)$$

$$\text{cov}(\boldsymbol{\varepsilon}_{i,j}, \boldsymbol{\varepsilon}_{i+l,j+m}) = \rho^{\sqrt{l^2+m^2}}\theta\boldsymbol{\Sigma}, \quad (6)$$

where $\boldsymbol{\Sigma}$ is the covariance matrix for $\mathbf{X}_{i,j}$, the parameter ρ describes the spatial dependency between neighboring pixels, $\theta, 0 \leq \theta \leq 1$, determines how much of the variation of $\mathbf{X}_{i,j}$ that is due to the noise $\boldsymbol{\varepsilon}_{i,j}$ and $C_{i,j}$ denotes the true, in reality unknown, class of the pixel.

For the classifications only three patterns (called X, L and T) of neighborhoods were allowed as proposed in Owen (1984). The neighborhoods considered consist of a pixel $t=(i,j)$ and its four nearest neighbors. Imposing compass directions on the grid of pixels gives the neighbors the labels Nt , Et , St and Wt . Formally, a pattern is a partition of the set $\{t, Nt, Et, St, Wt\}$. In the X-pattern all five pixels are of the same class. The L-type patterns consist of $\{Nt, t, Et\}$, $\{Wt, St\}$ and rotations of this pattern through multiples of 90 degrees, while the T-type patterns consist of $\{Nt\}$, $\{t, Et, St, Wt\}$ and rotations thereof. No other patterns are considered, as those rarely exist in reality.

For all of the estimations, training data of 50 pixel neighborhoods were taken from 100 maps to imitate the real situation. 100 maps were used, as the total size of these maps would then correspond to the size of a Landsat TM scene.

The pixels were classified to four different strata from the simulated spectral values \mathbf{X} ; the same age classes that were used for the simulation of the stand map. From the training data parameter estimations of the mean of each stratum, the covariance matrix and the spatial dependency parameter were derived. The spatial dependency parameter ρ was derived using a method described in Hjort *et al.* (1985). This method gave an unstable estimator but with clear signs of a value of ρ close to zero. It was possible to obtain the same result with the autocorrelation function of the simulated data. The spectral values were therefore assumed to be independent and $\rho=0$ was used. The independence assumption is required owing to the lack of a spatial dependency model for the spectral values.

Each pixel is assigned to the class with the highest posterior probability. The prior probabilities $\pi(k)$, $k=1,\dots,4$, were all 0.25 and the conditional probabilities $\pi(k|m)$, $k,m=1,\dots,4$, were estimated with the conditional frequencies from the training data. Equal probabilities for the priors were used instead of estimated priors as the classes with low frequencies are normally poorly represented with a Bayesian approach. With more equally sized classes the result of the stratified sampling is generally better.

4 Results

Two variants of classification were performed; one based on the spectral values DN_4 and DN_5 according to equation (2), and one based on $\ln DN_4$ and $\ln DN_5$. For both variants the classification results were of a similar nature, see *Tables 2* and *3* for the confusion matrices when the parameter setting best corresponding to real data (i.e. when the simulations were based on the empirical age distribution, the spatial dependency weight 0.8 and the average stand size 14.6) was used. In the classifications performed, the youngest stands were classified with a high accuracy but the older stands were classified with a rather high error rate. These results were expected owing to the well-known fact that predictions of wood volumes, based on remotely sensed data, give good results for sparse forests and poor results for dense forests. Since the two variants of classification produced similar results, we only used the one based on DN_4 and DN_5 for the creation of strata.

Confusion matrix from the Dirichlet cells approach

i,j	DN				$\ln DN$			
	1	2	3	4	1	2	3	4
1	0.733	0.160	0.051	0.057	0.751	0.143	0.052	0.054
2	0.123	0.470	0.223	0.185	0.148	0.457	0.225	0.170
3	0.033	0.277	0.260	0.430	0.041	0.279	0.273	0.408
4	0.012	0.154	0.222	0.612	0.015	0.157	0.238	0.591

Table 2

Confusion matrix from the standard Poisson lines process

i,j	DN				$\ln DN$			
	1	2	3	4	1	2	3	4
1	0.750	0.156	0.046	0.048	0.773	0.138	0.043	0.046
2	0.103	0.484	0.235	0.177	0.133	0.488	0.216	0.163
3	0.025	0.272	0.276	0.426	0.034	0.292	0.267	0.407
4	0.009	0.143	0.234	0.613	0.011	0.160	0.233	0.596

Table 3

The stratified sampling was performed, and compared to simple random sampling for some settings. The results, based on 1000 replicates, are shown in *Tables 4-7* with 100 times the average of the quotient between the variances of the stratified sampling and the simple random sampling, respectively, for the specific settings. The standard error of the average estimator of the quotient is presented in brackets in the tables. The gain in precision with proportional allocation, for both map techniques, with the empirical distribution (based on the proportions of each class in the NFI data) and an average stand size of 14.6 m³/hectare, was about 34% when the stratified sampling was compared with the simple random sampling without replacement.

Results from the Dirichlet cells approach, proportional allocation

weights	av.size: 7.3		av.size: 14.6		av.size: 29.2	
	0.9	0.8	0.9	0.8	0.9	0.8
empirical	68.25(0.033)	68.13(0.034)	66.62(0.049)	66.08(0.047)	65.52(0.069)	64.76(0.070)
more old forest	80.08(0.031)	79.76(0.032)	78.92(0.045)	78.09(0.045)	77.53(0.063)	76.94(0.065)
more young forest	59.40(0.034)	59.12(0.030)	57.64(0.042)	57.04(0.043)	56.32(0.059)	55.33(0.059)

Table 4

Results from the standard Poisson line process, proportional allocation

	av.size: 7.3		av.size: 14.6		av.size: 29.2	
weights	0.9	0.8	0.9	0.8	0.9	0.8
empirical	67.34(0.070)	67.24(0.073)	66.21(0.094)	65.99(0.096)	65.40(0.137)	65.13(0.135)
more old forest	79.16(0.065)	78.83(0.068)	78.09(0.091)	77.94(0.091)	77.63(0.128)	77.45(0.129)
more young forest	58.52(0.064)	58.00(0.067)	57.33(0.089)	57.19(0.090)	56.09(0.120)	55.91(0.116)

Table 5

Results from the Dirichlet cells approach, optimal allocation

	av.size: 7.3		av.size: 14.6		av.size: 29.2	
weights	0.9	0.8	0.9	0.8	0.9	0.8
empirical	66.89(0.037)	67.20(0.038)	64.68(0.057)	64.44(0.053)	62.93(0.081)	62.44(0.081)
more old forest	79.80(0.033)	79.54(0.034)	78.46(0.048)	77.66(0.048)	76.80(0.069)	76.30(0.070)
more young forest	56.46(0.040)	56.57(0.037)	53.73(0.052)	53.48(0.052)	51.53(0.072)	51.10(0.072)

Table 6

Results from the standard Poisson line process, optimal allocation

	av.size: 7.3		av.size: 14.6		av.size: 29.2	
weights	0.9	0.8	0.9	0.8	0.9	0.8
empirical	65.60(0.080)	65.95(0.081)	63.84(0.110)	63.63(0.111)	62.64(0.161)	62.36(0.158)
more old forest	78.71(0.069)	78.52(0.072)	77.45(0.099)	77.33(0.099)	76.77(0.141)	76.59(0.143)
more young forest	54.95(0.077)	54.80(0.079)	53.07(0.107)	53.05(0.107)	51.01(0.145)	50.89(0.141)

Table 7

To check whether the form of the stand affects the result, the two map techniques described in Section 3.1 were used. The results in *Tables 4 and 5* show a small difference for the parameter setting best corresponding to real data. For some other parameter settings the result of the proportional allocation does give a recognizable difference, indicating that the form of the stands does affect the results of the stratification. For all of the settings, the gain in precision for stratified sampling is more variable for the standard Poisson line process. The gain was more with smaller stands and less with larger stands in comparison with the Dirichlet cells approach. This is probably due to the more variable number of stands that the standard Poisson process approach causes.

The size was alternated at three levels, 7.3, 14.6 and 29.2 hectares/stand, where level 14.6 hectares/stand is the one best corresponding to the hypothetical area. A notable difference in results for both proportional and optimal allocation of the stratified sampling was obtained when the average stand size was alternated for all alternatives of the probability distribution of the classes. The average stand size does affect the results; the precision improves as the size of the stands increases.

To check the stability of the spatial dependency model, two different settings of weights were used. With these settings the results for the standard Poisson line process did differ slightly. On the other hand the results for the Dirichlet cells technique had a recognizable difference. It was concluded that badly chosen weights are likely to cause a smaller effect on the maps created with the Dirichlet cells approach.

When the stand class distribution was changed, the results showed a similar pattern for the stand form, the average stand size, and the spatial dependency model as for the empirical distribution. The gain for the stratified sampling compared to simple random sampling does

change though. When the youngest class had a higher probability the gain was larger, and when the probability was lower the gain was less. This depends mainly on different inclusion probabilities for the age classes but also marginally on better results of the classifications.

If the variances of the wood volumes for each stratum are known, or if it is possible to obtain a reliable estimate of them, the optimal allocation is advisable. In other cases the proportional allocation is often preferable. For the simulated remotely sensed data, the variance was low for the youngest age class whilst the other classes had a variance that was higher and similar. The difference between the optimal allocation and the proportional allocation for the simulated data was therefore substantial only for the case with more young forest. Proportional allocation is therefore recommended unless the inventory is performed in an area with a high proportion of young stands.

5 Discussion

The results show that stratified sampling, with remotely sensed data used as auxiliary information, gives better precision than simple random sampling without replacement. It should be kept in mind though that there are some assumptions included. Some of them are worth noting, and are discussed in this section.

The wood volumes were simulated pixelwise within each stand, based on NFI data, through a sampling approach with a simple model for the spatial correction used to correct the data for the spatial dependency between neighboring values. Owing to the difficulty of finding a parametric probability distribution that fits the data well, this empirical use of data seems to be a better alternative than simulation of values strictly from a parametric probability distribution. An alternative method of acquiring wood volumes would be to use a Kriging based approach, and to then simulate a number of plots in each stand and use them as support points for the rest of the plots in the stand. The other plots could then be given their value from a Kriging predictor and a spatially correlated random error according to a parametric or nonparametric family of probability distributions.

The spectral values were simulated pixelwise as a function of wood volume based on a regression function. The dependency between neighboring pixels of the sensor was not taken into account when the spectral reflectances were simulated. It is reasonable to assume that the results will change if a dependency between pixels is used for the spectral model. It is quite likely that the accuracy of the classification algorithm would increase and the noise level of the spectral signals would be lower. With such a construction the spatial dependency parameter, ρ , for the classifications would differ from zero and the classification algorithm would then have more usable information.

Systematic sampling is a sample design that is efficient, under some conditions, when closely placed units in the population are rather homogeneous, i.e. adjacent units tend to have similar values, and/or there exists a linear trend in the data. It has been shown in Ranney *et al.* (1987) that systematic sampling is preferable to simple random sampling for the Swedish NFI for the above reasons. Therefore it would be of interest to compare the stratified sampling, based on remotely sensed data, with the systematic sampling. However, to make these comparisons fair, more care has to be taken in the modeling of the data, e.g. in the current study there are no trends in the data (as could be expected when going from coast to mountain).

In the case of rare events, for example where 1-5% of the area is covered with the event,

there are also problems in the precise creation of a design and estimators. An example of a rare event in forestry applications is a clearcut area. To solve this rare event problem a design created with more variables than only wood volume could be of importance. Designs for rare events and multidimensional inventories are areas in which more research is necessary.

The simulations were coded in Fortran90 on a PC. They were also implemented on a parallel computer using a message passing system called MPI to send information between different processors.

6 Acknowledgements

The author thanks Professor Bo Ranney and Dr. Magnus Ekström, who have been very helpful during the study. The author also thanks Dr. Mats Nilsson and Jörgen Wallerman for valuable help with data and advice. Financial support was provided by NGSSC, the National Graduate School in Scientific Computing. This study is part of the Swedish Mistra project RESE, Remote Sensing for the Environment.

References

- Crain, I. K. and Miles, R. E. (1976). Monte Carlo estimates of the distributions of the random polygons determined by random lines in a plane. *J. Statist. Comput. Simul.* **4**, 293-325.
- Flygare, A-M. (1993). Contextual classification using multi-temporal Landsat TM data, Licentiate thesis, *Statistical Research Report* 1993-1995. University of Umeå.
- Goudsmit, S. A. (1945). Random distributions of lines in a plane. *Rev. Mod. Phys.* **17**, 321-322.
- Haslett, J. (1985). Maximum likelihood discriminant analysis on the plane using a Markovian model of spatial context. *Pattern Recognition* **18**, 287-296.
- Hjort, N.L., Mohn, E and Storvik, G. (1985). Contextual classification of remotely sensed data, based on an auto-correlation model. Project Report: "Contextual classification of remotely sensed data: statistical methods and developments of a system", Norwegian Computing Center, Oslo, Norway, Rep. 768.
- Kartikeyan, B., Gopalakrishna, B., Kalubarme, M.H. and Majumder, K.L. (1994). Contextual techniques for classification of high and low resolution remote sensing data. *Int. J. Remote Sensing* **15**, 1037-1051.
- Khazenie, N. and Crawford, M.M. (1990). Spatial-temporal autocorrelated model for contextual classification. *IEEE Transactions on Geoscience and Remote Sensing* **28**, 529-539.
- McRoberts, R. E., Wendt, D. G., Nelson, M.D. and Hansen, M. H. (2002) Using a land cover classification based on satellite imagery to improve the precision of forest inventory area estimates. *Remote Sensing of Environment* **81**, 36-44.
- Miles, R. E. (1964a). Random polygons determined by random lines in a plane. *Proceedings of the National Academy of Sciences of the United States of America* **52**, 901-907.
- Miles, R. E. (1964b). Random polygons determined by random lines in a plane, II. *Proceedings of the National Academy of Sciences of the United States of America* **52**, 1157-1160.
- Nilsson, M. and Ranneby, B. (1997). Estimation of wood volume using satellite spectral data - a simulation study, doctoral thesis. Swedish University of Agricultural Sciences, Faculty of Forestry, Uppsala, Sweden.
- Okabe, A., Boots, B. and Sugihara, K. (2000). *Spatial tessellations : concepts and applications of Voronoi diagrams*. Second edition, Chichester : Wiley, cop.
- Owen, A. (1984). A neighbourhood based classifier for Landsat data. *Canadian Journal of Statistics*. **12**, 191-200.
- Owen, A. and Switzer, P. (1982). A neighbourhood based classifier for Landsat data. *Technical report*. Department of Statistics, Stanford University.
- Poso, S., Paananen, R. and Simila, M. (1987). Forest inventory by compartments using satellite imagery. *Silva Fennica* **21**, 69-94.

Ranneby, B., Cruse, T., Hägglund, B., Jonasson, H. and Swärd, J. (1987). *Designing a new national forest survey for Sweden*. Swedish University of Agricultural Sciences, Faculty of Forestry, Uppsala, Sweden.

Santalo, L. A. (1979). *Integral geometry and geometric probability*. Second edition, Addison-Wesley Publishing Company, Inc.

Sharma, K.M.S. and Sarkar, A. (1998). A modified contextual classification technique for remote sensing data. *Photogrammetric Engineering and Remote Sensing* **64**, 273-280

Wallerman, J., Joyce, S., Vencatasawmy, C. and Olsson, H. (2002). Prediction of forest stem volume using kriging adapted to detected edges. *Canadian Journal of Forest Research*.**32**, 509-518

Watanabe, T., Suzuki, H., Tanba, S. and Yokohama, R. (1994). Improved contextual classifiers of multispectral data. *IEICE T. Fund. Electr.* **E77A**, 1445-1450

Serien Arbetsrapporter utges i första hand för institutionens eget behov av viss dokumentation. Rapporterna är indelade i följande grupper: Riksskogstaxeringen, Planering och inventering, Biometri, Fjärranalys, Kompendier och undervisningsmaterial, Examensarbeten samt internationellt. Författarna svarar själva för rapporternas vetenskapliga innehåll.

This series of Working Papers reflects the activity of this Department of Forest Resource Management and Geomatics. The sole responsibility for the scientific content of each Working Paper relies on the respective author.

Riksskogstaxeringen: (*The Swedish National Forest Inventory*)

- 1995 1 Kempe, G. Hjälpmedel för bestämning av slutenhet i plant- och ungskog. ISRN SLU-SRG-AR--1--SE
- 2 Riksskogstaxeringen och Ståndortskarteringen vid regional miljöövervakning. - metoder för att förbättra upplösningen vid inventering i skogliga avrinningsområden. ISRN SLU-SRG-AR--2--SE.
- 1997 23 Lundström, A., Nilsson, P. & Ståhl, G. Certifieringens konsekvenser för möjliga uttag av industri- och energived. - En pilotstudie. ISRN SLU-SRG-AR--23--SE.
- 24 Fridman, J. & Walheim, M. Död ved i Sverige. - Statistik från Riksskogstaxeringen. ISRN SLU-SRG-AR--24--SE.
- 1998 30 Fridman, J. & Kihlblom, D. & Söderberg, U. Förslag till miljöindexsystem för naturtypen skog. ISRN SLU-SRG-AR--30--SE.
- 34 Löfgren, P. Skogsmark, samt träd- och buskmark inom fjällområdet. En skattning av arealerenligt internationella ägoslagsdefinitioner. ISRN SLU-SRG-AR--34--SE.
- 37 Odell, G. & Ståhl, G. Vegetationsförändringar i svensk skogsmark mellan 1980- och 90-talet. -En studie grundad på Ståndortskarteringen. ISRN SLU-SRG-AR--37--SE.
- 38 Lind, T. Quantifying the area of edge zones in Swedish forest to assess the impact of nature conservation on timber yields. ISRN SLU-SRG-AR--38--SE.
- 1999 50 Ståhl, G., Walheim, M. & Löfgren, P. Fjällinventering. - En utredning av innehåll och design. ISRN SLU-SRG--AR--50--SE.
- 52 Riksskogstaxeringen inför 2000-talet. - Utredningar avseende innehåll och omfattning i en framtida Riksskogstaxering. Redaktörer: Jonas Fridman & Göran Ståhl. ISRN SLU-SRG-AR--52--SE.
- 54 Fridman, J. m.fl. Sveriges skogsmarksarealer enligt internationella ägoslagsdefinitioner. ISRN SLU-SRG-AR--54--SE.
- 56 Nilsson, P. & Gustafsson, K. Skogsskötseln vid 90-talets mitt - läge och trender. ISRN SLU-SRG-AR--56--SE.

- 57 Nilsson, P. & Söderberg, U. Trender i svensk skogsskötsel - en intervjuundersökning. ISRN SLU-SRG-AR--57--SE.
- 1999 61 Broman, N & Christoffersson, J. Mätfel i provträdsvariabler och dess inverkan på precision och noggrannhet i volymskattningar. ISRN SLU-SRG-AR--61--SE.
- 65 Hallsby, G m.fl. Metodik för skattning av lokala skogsbränsleresurser. ISRN SLU-SRG-AR--65--SE.
- 75 von Segebaden, G. Komplement till "RIKSTAXEN 75 ÅR". ISRN SLU-SRG-AR--75--SE.
- 2001 86 Lind, T. Kolinnehåll i skog och mark i Sverige - Baserat på Riksskogstaxeringens data. ISRN SLU-SRG-AR--86--SE

Inventering och planering: (*Forest inventory and planning*)

- 1995 3 Holmgren, P. & Thuresson, T. Skoglig planering på amerikanska västkusten - intryck från en studieresa till Oregon, Washington och British Columbia 1-14 augusti 1995. ISRN SLU-SRG-AR--3--SE.
- 4 Ståhl, G. The Transect Relascope - An Instrument for the Quantification of Coarse Woody Debris. ISRN SLU-SRG-AR--4--SE
- 1996 15 van Kerkvoorde, M. A sequential approach in mathematical programming to include spatial aspects of biodiversity in long range forest management planning. ISRN SLU-SRG-AR--15--SE.
- 1997 18 Christoffersson, P. & Jonsson, P. Avdelningsfri inventering - tillvägagångssätt och tidsåtgång. ISRN SLU-SRG-AR--18--SE.
- 19 Ståhl, G., Ringvall, A. & Lämås, T. Guided transect sampling - An outline of the principle. ISRN SLU-SRGL-AR--19--SE.
- 25 Lämås, T. & Ståhl, G. Skattning av tillstånd och förändringar genom inventerings-simulering - En handledning till programpaketet "NVSIM". ISRN SLU-SRG-AR--25--SE.
- 26 Lämås, T. & Ståhl, G. Om dektering av förändringar av populationer i begränsade områden. ISRN SLU-SRG-AR--26--SE.
- 1999 59 Petersson, H. Biomassafunktioner för trädfractioner av tall, gran och björk i Sverige. ISRN SLU-SRG-AR--59--SE.
- 63 Fridman, J., Löfstrand, R & Roos, S. Stickprovsvis landskapsövervakning - En förstudie. ISRN SLU-SRG-AR--63--SE.
- 2000 68 Nyström, K. Funktioner för att skatta höjdtillväxten i ungskog. ISRN SLU-SRG-AR--68--SE.

- 57 Nilsson, P. & Söderberg, U. Trender i svensk skogsskötsel - en intervjuundersökning. ISRN SLU-SRG-AR--57--SE.
- 1999 61 Broman, N & Christoffersson, J. Mätfel i provträdsvariabler och dess inverkan på precision och noggrannhet i volymskattningar. ISRN SLU-SRG-AR--61--SE.
- 65 Hallsby, G m.fl. Metodik för skattning av lokala skogsbränsleresurser. ISRN SLU-SRG-AR--65--SE.
- 75 von Segebaden, G. Komplement till "RIKSTAXEN 75 ÅR". ISRN SLU-SRG-AR--75--SE.
- 2001 86 Lind, T. Kolinnehåll i skog och mark i Sverige - Baserat på Riksskogstaxeringens data. ISRN SLU-SRG-AR--86--SE

Inventering och planering: (*Forest inventory and planning*)

- 1995 3 Holmgren, P. & Thuresson, T. Skoglig planering på amerikanska västkusten - intryck från en studieresa till Oregon, Washington och British Columbia 1-14 augusti 1995. ISRN SLU-SRG-AR--3--SE.
- 4 Ståhl, G. The Transect Relascope - An Instrument for the Quantification of Coarse Woody Debris. ISRN SLU-SRG-AR--4--SE
- 1996 15 van Kerkvoorde, M. A sequential approach in mathematical programming to include spatial aspects of biodiversity in long range forest management planning. ISRN SLU-SRG-AR--15--SE.
- 1997 18 Christoffersson, P. & Jonsson, P. Avdelningsfri inventering - tillvägagångssätt och tidsåtgång. ISRN SLU-SRG-AR--18--SE.
- 19 Ståhl, G., Ringvall, A. & Lämås, T. Guided transect sampling - An outline of the principle. ISRN SLU-SRGL-AR--19--SE.
- 25 Lämås, T. & Ståhl, G. Skattning av tillstånd och förändringar genom inventerings-simulering - En handledning till programpaketet "NVSIM". ISRN SLU-SRG-AR--25--SE.
- 26 Lämås, T. & Ståhl, G. Om dektering av förändringar av populationer i begränsade områden. ISRN SLU-SRG-AR--26--SE.
- 1999 59 Petersson, H. Biomassafunktioner för trädfraktioner av tall, gran och björk i Sverige. ISRN SLU-SRG-AR--59--SE.
- 63 Fridman, J., Löfstrand, R & Roos, S. Stickprovvis landskapsövervakning - En förstudie. ISRN SLU-SRG-AR--63--SE.
- 2000 68 Nyström, K. Funktioner för att skatta höjdtillväxten i ungskog. ISRN SLU-SRG-AR--68--SE.

- 70 Walheim, M. & Löfgren, P. Metodutveckling för vegetationsövervakning i fjällen. ISRN SLU-SRG-AR--70--SE.
- 73 Holm, S. & Lundström, A. Åtgärdsprioriteter. ISRN SLU-SRG-AR--73--SE.
- 76 Fridman, J. & Ståhl, G. Funktioner för naturlig avgång i svensk skog. ISRN SLU-SRG-AR--76--SE.
- 2001 82 Holmström, H. Averaging Absolute GPS Positionings Made Underneath Different Forest Canopies - A Splendid Example of Bad Timing in Research. ISRN SLU-SRG-AR--79--SE.
- 2002 91 Wilhelmsson, E. Forest use and its economic value for inhabitants of Skroven and Hakkas in Norrbotten. ISRN SLU-SRG-AR--91--SE.
- 94 Eriksson, O. m fl. Wood Supply From Swedish Forests Managed According to the FSC-standard. ISRN SLU-SRG-AR--94--SE.

Biometri: (*Biometrics*)

- 1997 22 Ali, Abdul Aziz. Describing Tree Size Diversity. ISRN SLU-SRG-AR--22--SE.
- 1999 64 Berhe, L. Spatial continuity in tree diameter distribution. ISRN SLU-SRG-AR--64--SE
- 2001 88 Ekström, M. Nonparametric Estimation of the Variance of Sample Means Based on Nonstationary Spatial Data. ISRN SLU-SRG-AR--88--SE.
- 89 Ekström, M. & Belyaev, Y. On the Estimation of the Distribution of Sample Means Based on Non-Stationary Spatial Data. ISRN SLU-SRG-AR--89--SE.
- 90 Ekström, M. & Sjöstedt-de Luna, S. Estimation of the Variance of Sample Means Based on Nonstationary Spatial Data with Varying Expected Values. ISRN SLU-SRG-AR--90--SE.
- 2002 96 Norström, F. Forest inventory estimation using remotely sensed data as a stratification tool - a simulation study. ISRN SLU-SRG-AR--96--SE.

Fjärranalys: (*Remote Sensing*)

- 1997 28 Hagner, O. Satellitfjärranalys för skogsföretag. ISRN SLU-SRG-AR--28--SE.
- 29 Hagner, O. Textur till flygbilder för skattning av beståndsegenskaper. ISRN SLU-SRG-AR--29--SE.
- 1998 32 Dahlberg, U., Bergstedt, J. & Pettersson, A. Fälthinstruktion för och erfarenheter från vegetationsinventering i Abisko, sommaren 1997. ISRN SLU-SRG-AR--32--SE.
- 43 Wallerman, J. Brattåkerinventeringen. ISRN SLU-SRG-AR--28--SE.

- 1999 51 Holmgren, J., Wallerman, J. & Olsson, H. Plot - Level Stem Volume Estimation and Tree Species Discrimination with Casi Remote Sensing. ISRN SLU-SRG-AR--51--SE.
- 53 Reese, H. & Nilsson, M. Using Landsat TM and NFI data to estimate wood volume, tree biomass and stand age in Dalarna. ISRN SLU-SRG-AR--53--SE.
- 2000 66 Lofstrand, R., Reese, H. & Olsson, H. Remote Sensing aided Monitoring of Non-Timber Forest Resources - A literature survey. ISRN SLU-SRG-AR--66--SE.
- 69 Tingelöf, U & Nilsson, M. Kartering av hyggeskanter i pankromaötiska SPOT-bilder. ISRN SLU-SRG-AR--69--SE.
- 79 Reese, H & Nilsson, M. Wood volume estimations for Älvsbyn Kommun using SPOT satellite data and NFI plots. ISRN SLU-SRG-AR--79--SE.

Kompendier och undervisningsmaterial: (*Compendia and educational papers*)

- 1996 14 Holm, S. & Thuresson, T. samt jägm.studenter kurs 92/96. En analys av skogsstillståndet samt några alternativa avverkningsberäkningar för en del av Östads säteri. ISRN SLU-SRG-AR--14--SE.
- 21 Holm, S. & Thuresson, T. samt jägm.studenter kurs 93/97. En analys av skogsstillståndet samt några alternativa avverkningsberäkningar för en stor del av Östads säteri. ISRN SLU-SRG-AR--21--SE.
- 1998 42 Holm, S. & Lämås, T. samt jägm.studenter kurs 93/97. An analysis of the state of the forest and of some management alternatives for the Östad estate. ISRN SLU-SRG-AR--42--SE
- 1999 58 Holm, S. samt studenter vid Sveriges lantbruksuniversitet i samband med kurs i strategisk och taktisk skoglig planering år 1998. En analys av skogsstillståndet samt några alternativa avverknings beräkningar för Östads säteri. ISRN SLU-SRG-AR--58--SE.
- 2001 87 Eriksson, O. (Ed.) Strategier för Östads säteri: Redovisning av planer framtagna under kursen Skoglig planering ur ett företagsperspektiv HT2000, SLU Umeå. ISRN SLU-SRG-AR--87--SE..
- 2002 93 Lind, T. (Ed.) Strategier för Östads säteri: Redovisning av planer framtagna under kursen Skoglig planering ur ett företagsperspektiv HT2001, SLU Umeå. ISRN SLU-SRG-AR--93--SE..

Examensarbeten: (*Theses by Swedish forestry students*)

- 1995 5 Törnquist, K. Ekologisk landskapsplanering i svenskt skogsbruk - hur började det?. Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--5--SE.

- 1996 6 Persson, S. & Segner, U. Aspekter kring datakvaliténs betydelse för den kortsiktiga planeringen. Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--6--SE.
- 7 Henriksson, L. The thinning quotient - a relevant description of a thinning? Gallringskvot - en tillförlitlig beskrivning av en gallring? Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--7--SE.
- 8 Ranvald, C. Sortimentinriktad avverkning. Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--8--SE.
- 9 Olofsson, C. Mångbruk i ett landskapsperspektiv - En fallstudie på MoDo Skog AB, Örnsköldsviks förvaltning. Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--9--SE.
- 10 Andersson, H. Taper curve functions and quality estimation for Common Oak (*Quercus Robur L.*) in Sweden. Examensarbete i ämnet skogsuppskattning och skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--10--SE.
- 11 Djurberg, H. Den skogliga informationens roll i ett kundanpassat virkesflöde. - En bakgrundsstudie samt simulering av inventeringsmetoders inverkan på noggrannhet i leveransprognoser till sågverk. Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--11--SE.
- 12 Bredberg, J. Skattning av ålder och andra beståndsvariabler - en fallstudie baserad på MoDo:s indelningsrutiner. Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--12--SE.
- 13 Gunnarsson, F. On the potential of Kriging for forest management planning. Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--13--SE.
- 16 Tormalm, K. Implementering av FSC-certifiering av mindre enskilda markägares skogsbruk. Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--16--SE.
- 1997 17 Engberg, M. Naturvärden i skog lämnad vid slutavverkning. - En inventering av upp till 35 år gamla föryngringsytor på Sundsvalls arbetsomsåde, SCA. Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN-SLU-SRG-AR--17--SE.
- 20 Cedervind, J. GPS under krontak i skog. Examensarbete i ämnet skogsuppskattning och skogsindelning. ISRN SLU-SRG-AR--20--SE.
- 27 Karlsson, A. En studie av tre inventeringsmetoder i slutavverkningsbestånd. Examensarbete. ISRN SLU-SRG-AR--27--SE.
- 1998 31 Bendz, J. SÖDRAs gröna skogsbruksplaner. En uppföljning relaterad till SÖDRAs miljömål, FSC's kriterier och svensk skogspolitik. Examensarbete. ISRN SLU-SRG-AR--31--SE.

- 33 Jonsson, Ö. Trädskikt och ståndortsförhållanden i strandskog. - En studie av tre bäckar i Västerbotten. Examensarbete. ISRN SLU-SRG-AR--33--SE.
- 35 Claesson, S. Thinning response functions for single trees of Common oak (*Quercus Robur L.*) Examensarbete. ISRN SLU-SEG-AR--35--SE.
- 36 Lindskog, M. New legal minimum ages for final felling. Consequences and forest owner attitudes in the county of Västerbotten. Examensarbete. ISRN SLU-SRG-AR--36--SE.
- 40 Persson, M. Skogsmarksindelningen i gröna och blå kartan - en utvärdering med hjälp av riksskogstaxeringens provtytor. Examensarbete. ISRN SLU-SRG-AR--40--SE.
- 41 Eriksson, F. Markbaserade sensorer för insamling av skogliga data - en förstudie. Examensarbete. ISRN SLU-SRG-AR--41--SE.
- 45 Gessler, C. Impedimentens potentiella betydelse för biologisk mångfald. - En studie av myr- och bergimpediment i ett skogslandskap i Västerbotten. Examensarbete. ISRN SLU-SRG-AR--45--SE.
- 46 Gustafsson, K. Långsiktplanering med geografiska hänsyn - en studie på Bräcke arbetsområde, SCA Forest and Timber. Examensarbete. ISRN SLU-SRG-AR--46--SE.
- 47 Holmgren, J. Estimating Wood Volume and Basal Area in Forest Compartments by Combining Satellite Image Data with Field Data. Examensarbete i ämnet Fjärranalys. ISRN SLU-SRG-AR--47--SE.
- 49 Härdelin, S. Framtida förekomst och rumslig fördelning av gammal skog. - En fallstudie på ett landskap i Bräcke arbetsområde. Examensarbete SCA. ISRN SLU-SRG-AR--49--SE.
- 1999 55 Imamovic, D. Simuleringsstudie av produktionskonsekvenser med olika miljömål. Examensarbete för Skogsstyrelsen. ISRN SLU-SRG-AR--55--SE
- 62 Fridh, L. Utbytesprognoser av rotstående skog. Examensarbete i skoglig planering. ISRN SLU-SRG-AR--62--SE.
- 2000 67 Jonsson, T. Differentiell GPS-mätning av punkter i skog. Point-accuracy for differential GPS under a forest canopy. ISRN SLU-SRG-AR--67--SE.
- 71 Lundberg, N. Kalibrering av den multivariata variabeln trädslagsfördelning. Examensarbete i biometri. ISRN SLU-SRG-AR--71--SE.
- 72 Skoog, E. Leveransprecision och ledtid - två nyckeltal för styrning av virkesflödet. Examensarbete i skoglig planering. ISRN SLU-SRG-AR--72--SE.
- 74 Johansson, L. Rotröta i Sverige enligt Riksskogstaxeringen. Examensarbete i ämnet skogsindelning och skogsuppskattning. ISRN SLU-SRG-AR--74--SE.

- 77 Nordh, M. Modellstudie av potentialen för renbete anpassat till kommande slutavverkningar. Examensarbete på jägmästarprogrammet i ämnet skoglig planering. ISRN SLU-SRG-AR--77--SE.
- 78 Eriksson, D. Spatial Modeling of Nature Conservation Variables useful in Forestry Planning. Examensarbete. ISRN SLU-SRG-AR--74--SE.
- 81 Fredberg, K. Landskapsanalys med GIS och ett skogligt planeringssystem. Examensarbete på skogsvetarprogrammet i ämnet skogshushållning. ISRN SLU-SRG-AR--81--SE.
- 2001 83 Lindroos, O. Underlag för skogligt länsprogram Gotland. Examensarbete i ämnet skoglig planering. ISRN SLU-SRG-AR--83--SE.
- 84 Dahl, M. Satellitbildsbaserade skattningar av skogsområden med röjningsbehov. Examensarbete på skogsvetarprogrammet i ämnet skoglig planering. ISRN SLU-SRG-AR--84--SE.
- 85 Staland, J. Styrning av kundanpassade timmerflöden - Inverkan av traktbankens storlek och utbytesprognosens tillförlitlighet. Examensarbete i ämnet skoglig planering. ISRN SLU-SRG-AR--85--SE.
- 2002 92 Bodenhem, J. Tillämpning av olika fjärranalysmetoder för urvalsförfarandet av ungskogsbestånd inom den enkla älgbetesinventeringen (ÄBIN). Examensarbete på skogsvetarprogrammet i ämnet fjärranalys. ISRN SLU-SRG-AR--92--SE.
- 95 Sundquist, S. Development of a measure of production density for the Swedish National Forest Inventory. ISRN SLU-SEG-AR--95--SE.

Internationellt: (*International issues*)

- 1998 39 Sandewall, Ohlsson, B & Sandewall, R.K. People's options on forest land use - a research study of land use dynamics and socio-economic conditions in a historical perspective in the Upper Nam Nan Water Catchment Area, Lao PDR. ISRN SLU-SRG-AR--39--SE.
- 44 Sandewall, M., Ohlsson, B., Sandewall, R.K., Vo Chi Chung, Tran Thi Binh & Pham Quoc Hung. People's options on forest land use. Government plans and farmers intentions - a strategic dilemma. ISRN SLU-SRG-AR--44--SE.
- 48 Sengthong, B. Estimating Growing Stock and Allowable Cut in Lao PDR using Data from Land Use Maps and the National Forest Inventory (NFI). Master thesis. ISRN SLU-SRG-AR--48--SE.
- 1999 60 Inter-active and dynamic approaches on forest and land-use planning - proceedings from a training workshop in Vietnam and Lao PDR, April 12-30, 1999. Edited by Mats Sandewall ISRN SLU-SRG-AR--60--SE.
- 2000 80 Sawathvong, S. Forest Land Use Planning in Nam Pui National Biodiversity Conservation Area, Lao P.D.R. ISRN SLU-SRG-AR--80--SE.